

Reg.	No.	:			 											

Name :

Fourth Semester B.Tech. Degree Examination, February 2015 (2008 Scheme)

08.401 : ENGINEERING MATHEMATICS - III (CMPUNERFHB)
(Special Supplementary)

Time: 3 Hours Max. Marks: 100

Answer all questions from Part A and one full question from each Module of Part B.

PART-A

- 1. Show that Suiz is analytic every where in the complex plane and find its derivative.
- 2. Examine whether $xy^2 + x^2y$ can be the real part of an analytic function.
- 3. If a function is analytic show that it is independent of \bar{z} .
- 4. Find the image of the half plane x < c under the mapping w = 1/z.
- 5. Using Cauchy's integral formula evaluate $\int_{c}^{dz} \frac{dz}{z^2+4}$ where c is the circle |z-i|=2.
- 6. Expand $\frac{z-1}{z^2}$ as a Taylar series in powers of z-1 and state the region of convergence.
- 7. Find the poles and residues of $\frac{\text{suiz}}{z^4}$.
- 8. Solve the equations by Gauss Elimination method

$$2x + 3y - z = 5$$

$$4x + 4y - 3z = 3$$

$$2x - 3y + 2z = 2$$



- 9. Fit a polynomial to the data
 - x: 0 1 3
 - y:-12 0 6 12
- 10. Use Trapezoidal rule to evaluate $\int_{0}^{1} \frac{1}{1+x^2} dx$ with h = 0.5 and hence deduce an approximate value of π . (10×4=40 Marks)

Module - 1 '

- 11. a) Prove that the function $F(z) = \frac{x^3(1+i) y^3(1-i)}{x^2 + y^2}$ when $z \neq 0$, F(z) = 0. When z = 0 is not analytic at z = 0 even though Cauchy-Riemann equations are satisfied at that point.
 - b) Construct the analytic function whose real part is $\sin x \cosh y + 2 \cos x \sinh y + x^2 y^2 + 4xy$.
 - c) Find the bilinear transformation which maps the points z=0, i, 2i into the points w=5i, ∞ , $\frac{i}{3}$.
- 12. a) Find the analytic function F(z) = u + iv if $u + v = \frac{x}{x^2 + y^2}$ and F(1) = 1.
 - b) What is the image of the circle |z| = c under the transformation $w = z + \frac{1}{z}$?

 Discuss the case when c = 1.
 - c) If F(z) is analytic, show that

$$\nabla^2 |F(z)|^2 = 4 |F'(z)|^2$$



Module - II

- 13. a) Evaluate $\int_{c} |z|^2 dz$ where c is the rectangle with vertices z = 0, z = 1, z = 1 + i and z = i.
 - b) Obtain the Laurent's series expansion of the function $\frac{1}{z-z^3}$ in the region 1 < |z+1| < 2.
 - c) Evaluate $\int_{c} \frac{z-2}{z(z-1)} dz$ where c is the circle |z|=2 using Residue theorem.
- 14. a) Show that $\int_{0}^{2\pi} \frac{d\theta}{1 + k \cos \theta} = \frac{2\pi}{\sqrt{1 k^2}} (k^2 < 1)$



b) Evaluate $\int_{0}^{\infty} \frac{dx}{x^4 + 1}$.

Module - III

- 15. a) Find the root of $xe^x 2 = 0$ which lies between 0 and 1 to four decimal places using the method of false position.
 - b) Using Gauss Seidal method solve the following system of equations.

$$w - x + 3y - 3z = 3$$

$$2w + 3x + y - 11z = 1$$

$$5w - 2x + 5y - 4z = 5$$

$$3w + 4x - 7y + 2z = -7$$

c) Estimate the value of F(22) from the following table

x:

20

25

30

35

4(

F(x):

354

332

291

260

231

204

45



16. a) The following table gives the velocity 'v' of a particle at time 't'.

t (seconds)	0	2	4	6	8	10	12
v (metres/sec)	4	6	16	34	60	94	136

Using Simpson's method, find the distance moved by the particle in 12 seconds.

b) Find y(.2) and y(.3) by Taylor's series method if

$$y' + y = x^2, y(0) = 1$$

c) Solve $\frac{dy}{dx} = \frac{3x+y}{2}$, y(0) = 1 using Range-Kutta method of order 4 and find y (.2).

(3×20=60 Marks)

